

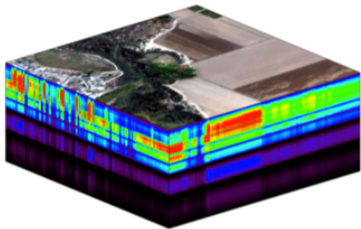
# AI systems for computer vision: Challenges in high-dimensional and multimodal image analysis

Aleksandra Pižurica

Group for Artificial Intelligence and Sparse Coding (GAIM)  
Department Telecommunications and Information Processing  
Ghent University

AI FOR PHOTONICS  
NB Photonics Topical Meeting  
February 5 2021

# A Wealth of High-Dimensional Multimodal Data



Remote sensing data (hyperspectral, visible, LiDAR,...)



Digitized paintings (infrared, X-Ray, visible)

# Hyperspectral Imaging (HSI) in Earth observation

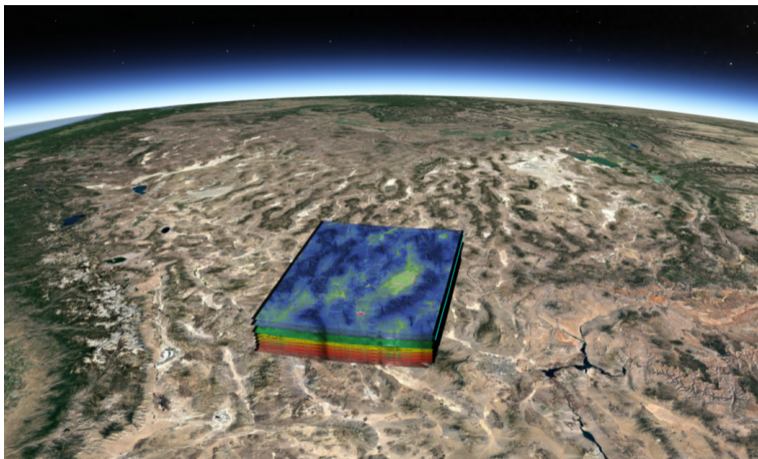
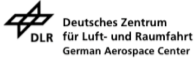


Image credit: Novus Light Technologies Today, December 2018.

HyperScout1 – the first miniaturized hyperspectral imager for space. Launched to an orbit 540km above the Earth. (ESA program, led by Cosine Measurement Systems)

# HSI space technology - game changer in environmental monitoring



29. June 2018

News /

## Hyperspectral Earth observation instrument DESIS sets off for the ISS



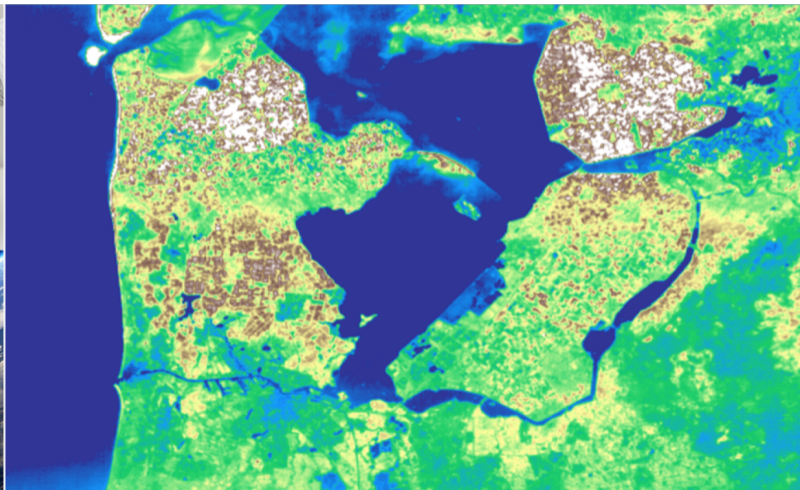
DESIS - Hyperspectral Earth Observation Instrument on the ISS  
Image 2/2, Credit: DLR (CC-BY 3.0)



DLR Earth Sensing Imaging Spectrometer (DESIS) installed on the International Space Station (ISS). Monitors environmental changes on Earth.

# “Milk-carton-sized HyperScout making hyperspectral Earth views”

Space news feed, 20 May 2020

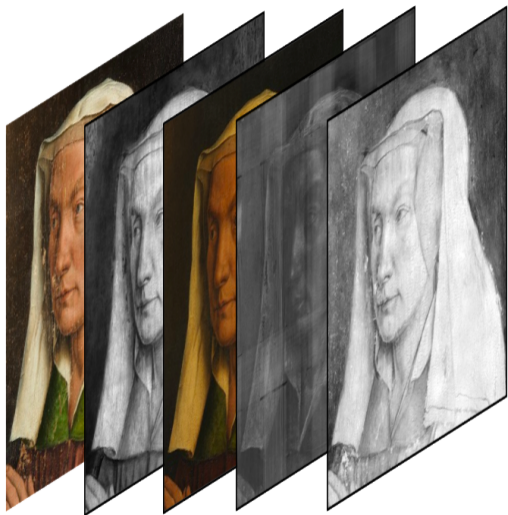


HyperScout view of Netherlands (courtesy: cosine)

# Multimodal data analysis in art investigation

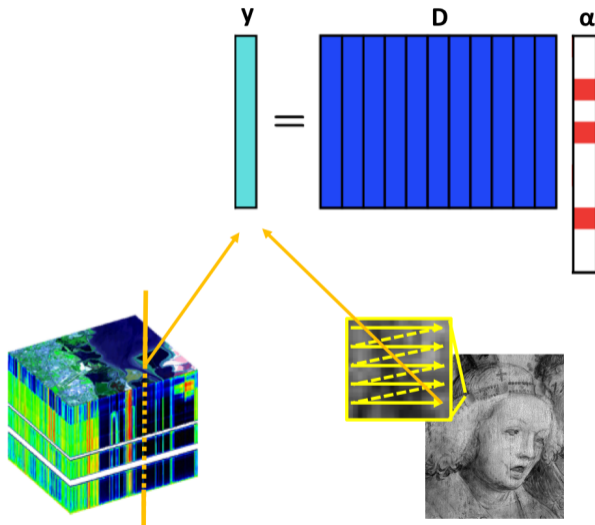
Extracting useful information from multiple modalities, with

- huge data
- imperfect alignment
- scarce annotations
- erroneous annotations



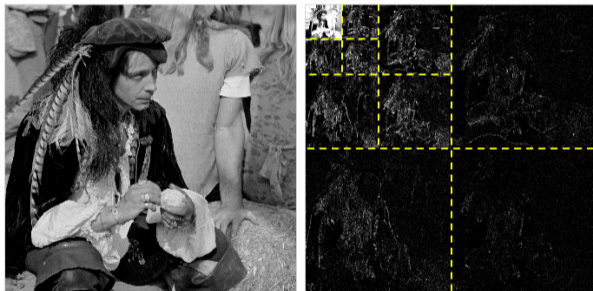
©Ghent, Kathedrale Kerkfabriek, Lukasweb

# Sparse representation



# Designed vs. Learned Dictionaries

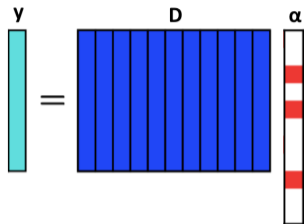
- **Designed dictionaries:** wavelets, curvelets, shearlets...
  - ▶ typically yield sparse representation of signals and images
  - ▶ advantages: generic, fast computation



- **Learned dictionaries**
  - ▶ trained on a set of representative examples
  - ▶ goal: optimally sparse representation for a given class of signals



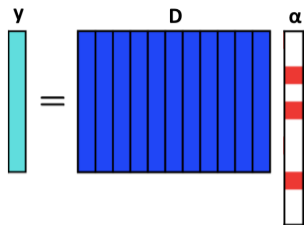
# Sparse coding



$$\hat{\alpha} = \arg \min_{\alpha} \|y - D\alpha\|_2^2 \quad \text{subject to} \quad \|\alpha\|_0 \leq K$$

$$\hat{\alpha} = \arg \min_{\alpha} \|\alpha\|_0 \quad \text{subject to} \quad \|y - D\alpha\|_2^2 \leq \epsilon$$

# Sparse coding



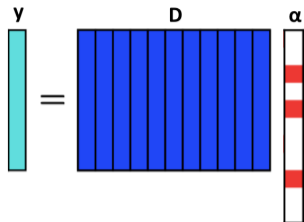
$$\hat{\alpha} = \arg \min_{\alpha} \|y - D\alpha\|_2^2 \quad \text{subject to} \quad \|\alpha\|_0 \leq K$$

$$\hat{\alpha} = \arg \min_{\alpha} \|\alpha\|_0 \quad \text{subject to} \quad \|y - D\alpha\|_2^2 \leq \epsilon$$

## Greedy algorithms

- **Matching Pursuit (MP)** [Mallat and Zhang, '93]
- **OMP** [Tropp, '04], **CoSaMP** [Needell and Tropp, '09]
- **IHT** [Blumensath and Davies, 09]

## Sparse coding



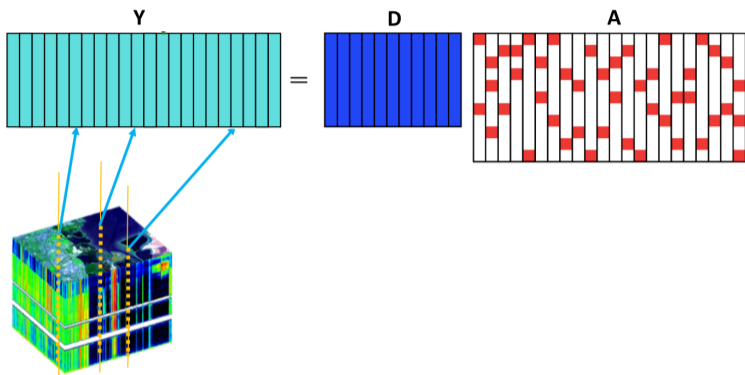
### Convex relaxation:

$$\hat{\alpha} = \arg \min_{\alpha} \|\alpha\|_1 \quad \text{subject to} \quad \|y - D\alpha\|_2^2 \leq \epsilon$$

$$\hat{\alpha} = \arg \min_{\alpha} \|y - D\alpha\|_2^2 + \lambda \|\alpha\|_1$$

**LASSO** [Tibshirani, '96], **BPDN** [Chen et al, '01]

# Sparse coding and dictionary learning

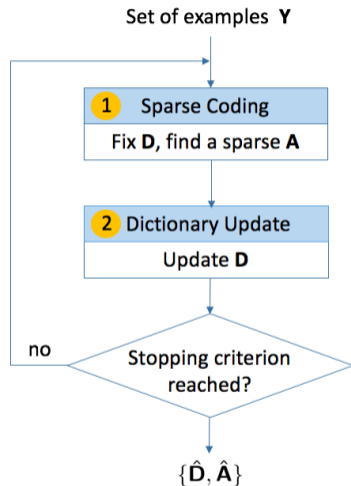


$$\{\hat{D}, \hat{A}\} = \arg \min_{D, A} \left\{ \|Y - DA\|_F^2 \right\} \quad \text{subject to} \quad \forall i, \|\alpha_i\|_0 \leq K$$

A similar objective:

$$\{\hat{D}, \hat{A}\} = \arg \min_{D, A} \sum \|\alpha_i\|_0 \quad \text{subject to} \quad \|Y - DA\|_F^2 \leq \epsilon$$

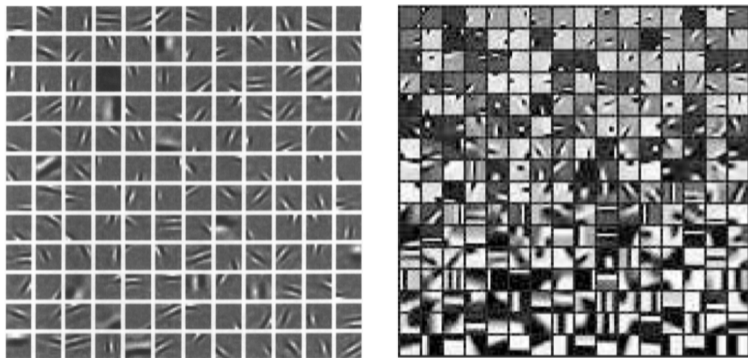
# Iterate Two Steps: Sparse Coding and Dictionary Update



Dictionary update:

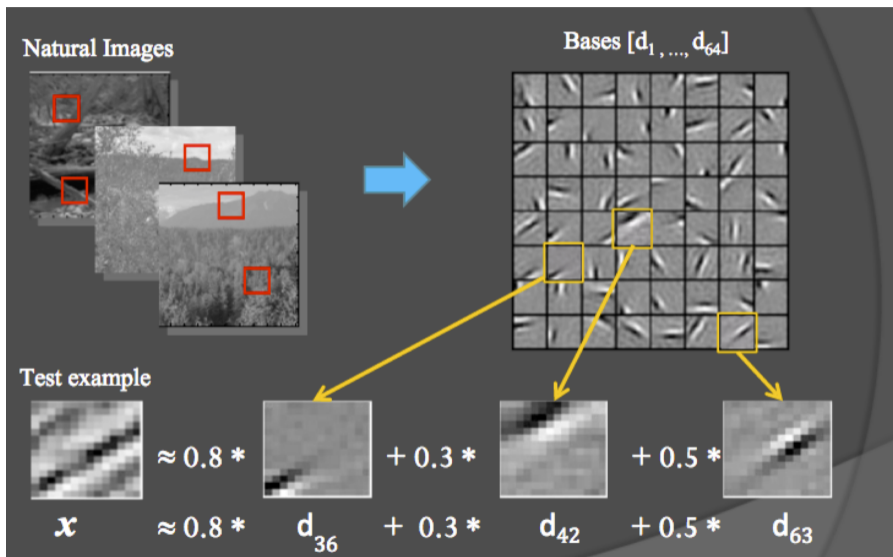
- Maximum likelihood method of [Olshausen and Field, 1997]
- MOD [Engan et al., 1999]
- K-SVD [Aharon et al., 2006]

## Learned Dictionaries of Image Atoms - Examples

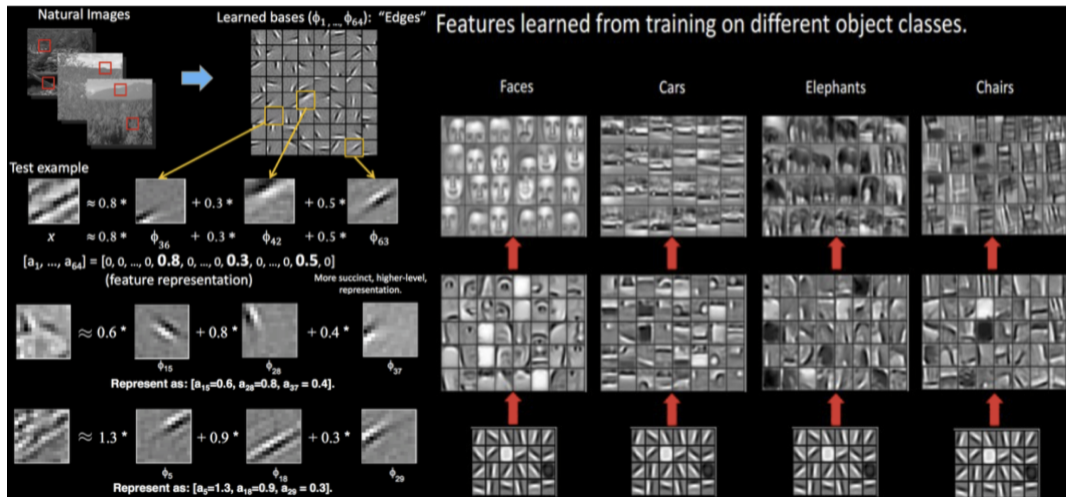


Examples of dictionaries trained by [Olshausen and Field, 1997] (left) and K-SVD [Aharon et al., 2006] (right)

# Representation learning and sparse coding



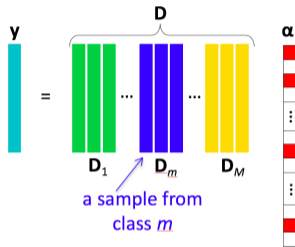
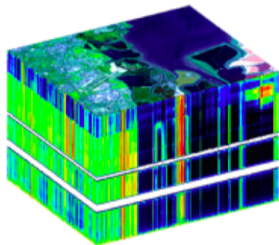
# Representation learning and sparse coding





# Sparse Representation Classification

[Wright et al, 2009]



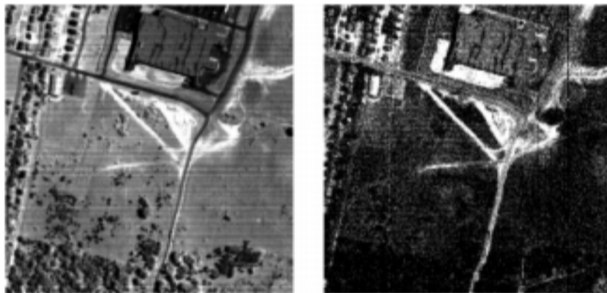
$$\hat{\alpha} = \arg \min_{\alpha} \|y - D\alpha\|_2^2 \quad \text{subject to } \|\alpha\|_0 \leq K$$

$$r_m(y) = \|y - D_m \hat{\alpha}_m\|_2, \quad m = 1, \dots, M$$

$$\text{class}(y) = \arg \min_{m=1, \dots, M} r_m(y)$$

# Robust SRC for Hyperspectral Image Classification

$$Y = \underbrace{X}_{\text{ideal image}} + \underbrace{N}_{\text{Gaussian noise}} + \underbrace{S}_{\text{sparse noise}}$$



Examples of stripe noise and mixed noise in a real hyperspectral image.

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Huang, S., Zhang, H., Liao, W., and Pižurica, A. (2017). Robust joint sparsity model for hyperspectral image classification. In IEEE ICIP 2017.

# Robust SRC for Hyperspectral Image Classification

$$Y = \underbrace{X}_{\text{ideal image}} + \underbrace{N}_{\text{Gaussian noise}} + \underbrace{S}_{\text{sparse noise}}$$

$$\{\hat{A}, \hat{S}\} = \arg \min_{A, S} \|Y - DA - S\|_F^2 + \lambda \|S\|_1 \quad \text{subject to} \quad \|A\|_{\text{row},0} \leq K$$

$$r_m(Y) = \|Y - D_m \hat{A}_m - \hat{S}\|_F, \quad m = 1, \dots, M$$

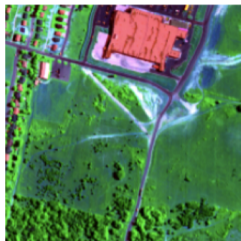
$$\text{class}(y_{\text{central}}) = \arg \min_{m=1, \dots, M} r_m(Y)$$

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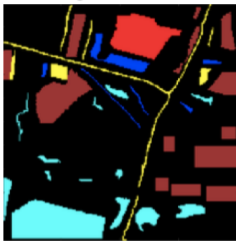
S. Huang, H. Zhang and A. Pižurica (2017). A Robust Sparse Representation Model for Hyperspectral Image Classification. *Sensors*.

# Robust SRC for Hyperspectral Image Classification

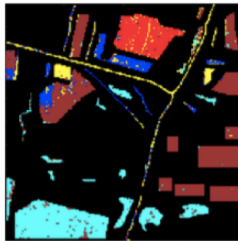
urban HYDICE (false color image)



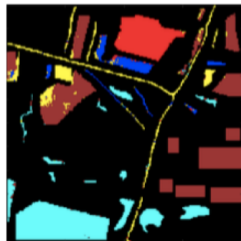
ground truth



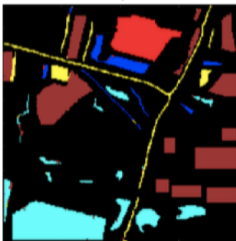
SVM, OA=89.0%



JSRC, OA=95.3%



our method, OA=98.7%



- Trees
- Concrete
- Soil
- Grass
- Asphalt

# Robust SRC for Hyperspectral Image Classification

Indian Pines (false color image)



ground truth



SVM, OA=80.4%



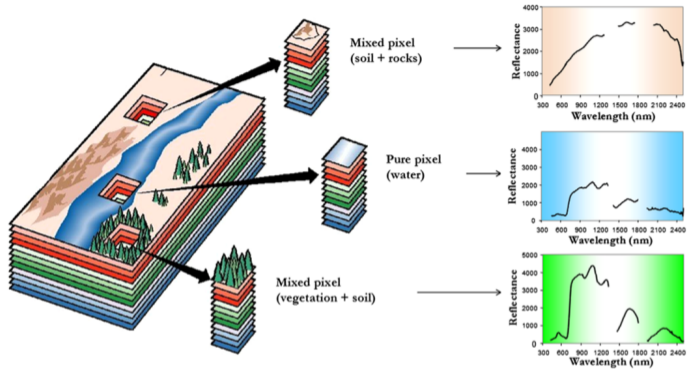
JSRC, OA=89.1%



our method, OA=96.9%

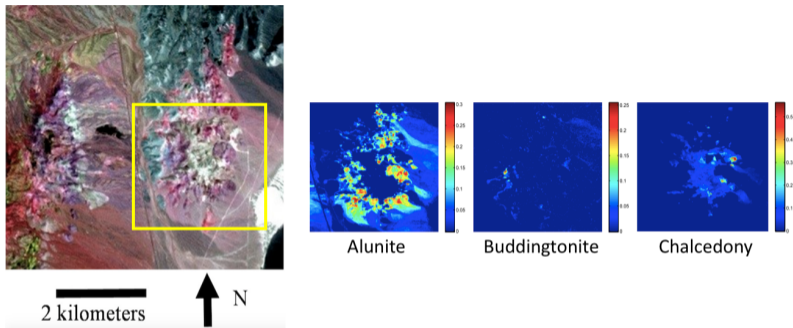


# Spectral Unmixing



S.R Bijitha, P. Geetha and K.P. Soman (2016). Performance Analysis and Comparative Study of Geometrical Approaches for Spectral Unmixing. International Journal of Scientific and Engineering Research.

# Sparse Unmixing

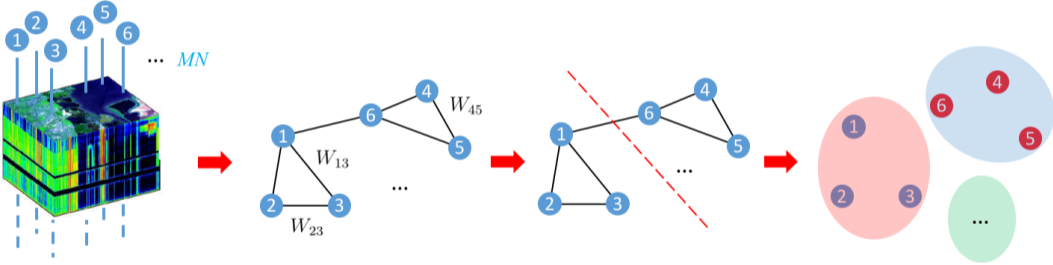


Estimated fractional abundance maps (AVIRIS Cuprite subscene, USGS library).

R. Wang, H.-C. Li, A. Pižurica, J. Li, A. Plaza, and W. J. Emery (2017). Hyperspectral Unmixing Using Double Reweighted Sparse Regression and Total Variation. *IEEE Geoscience and Remote Sensing Letters*.

# Spectral clustering

No labelled data available → no supervised classification but instead **clustering**



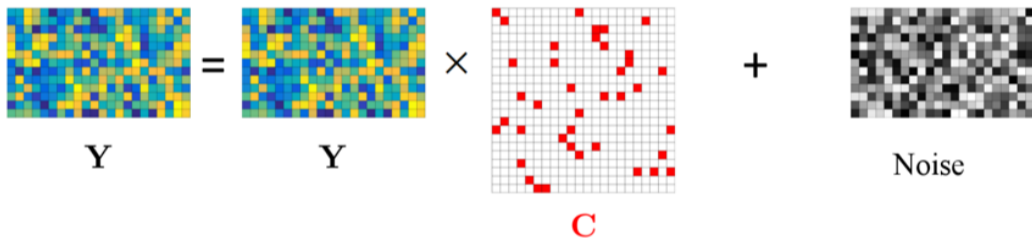
Similarity matrix:  $\mathbf{W} \in \mathbb{R}^{MN \times MN}$



# Sparse Subspace Clustering

[Elhamifar and Vidal, 2013]

Self-representation model:  $Y = YC + N$ ;  $Y = [y_1 \dots y_N] \in \mathbb{R}^{m \times N}$



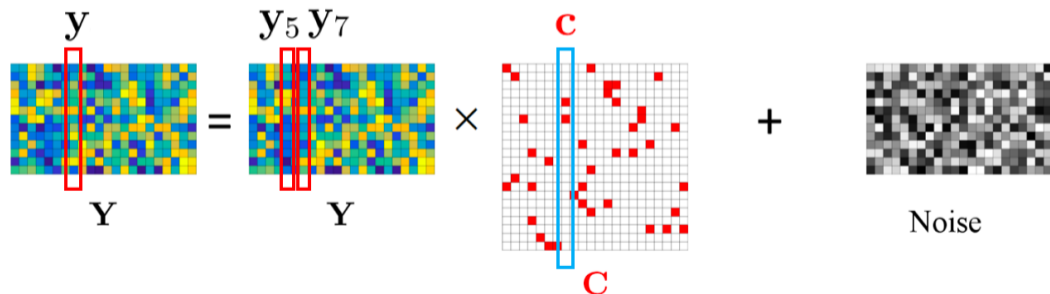
$C_{i,j} \neq 0 \rightarrow y_i$  and  $y_j$  are in the same subspace.

Similarity matrix:  $W = |C| + |C|^T$

# Sparse Subspace Clustering

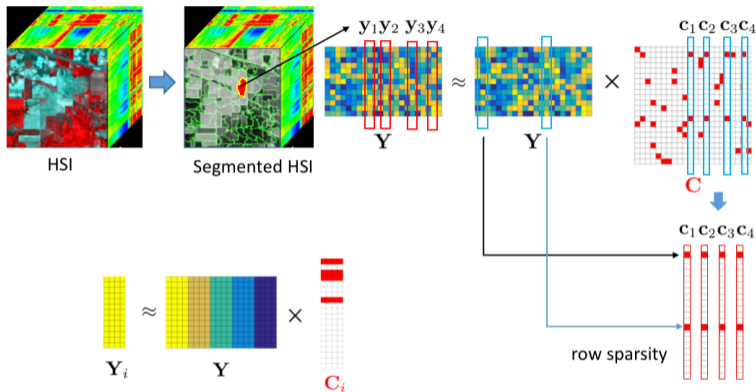
[Elhamifar and Vidal, 2013]

Self-representation model:  $Y = YC + N$ ;  $Y = [y_1 \dots y_N] \in \mathbb{R}^{m \times N}$



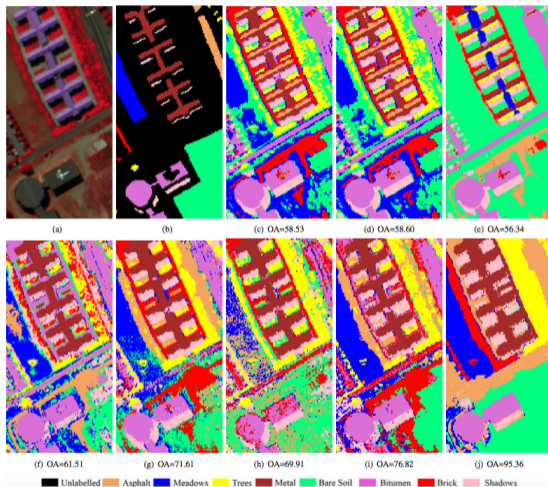
$$y \approx Yc = \sum_i y_i c_i = c_5 y_5 + c_7 y_7$$

# Joint Sparse Subspace Clustering - JSSC



S. Huang, H. Zhang and A. Pižurica (2019). Semi-supervised Sparse Subspace Clustering Method With a Joint Sparsity Constraint for Hyperspectral Remote Sensing Images. IEEE J. Sel. Topics in Earth Observation and Remote Sens.

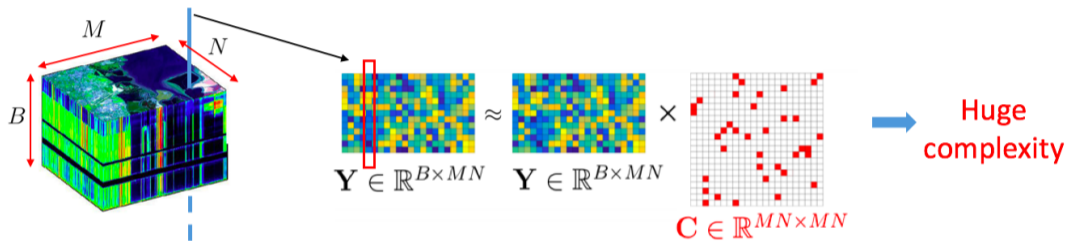
# Joint Sparse Subspace Clustering - JSSC



Pavia University image. (a) False color image, (b) Ground truth (c) FCM, (d) k-means, (e) CFSFDP, (f) SSC, (g) L2-SSC, (h) CPPSSC (1 % labelled samples), (i) JSSC and (j) JSSC-L (1% labelled samples)

[Huang et al., 2019]

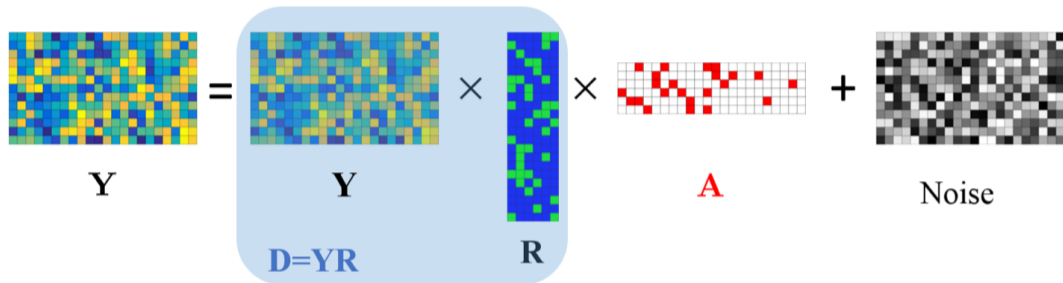
Nice, but ...



SSC becomes practically infeasible for **very large scale data**.

E.g. for the full *Pavia University* image  $610 \times 340$ , the size of  $C$  is  $207400 \times 207400$   
→ 320,5 GB memory

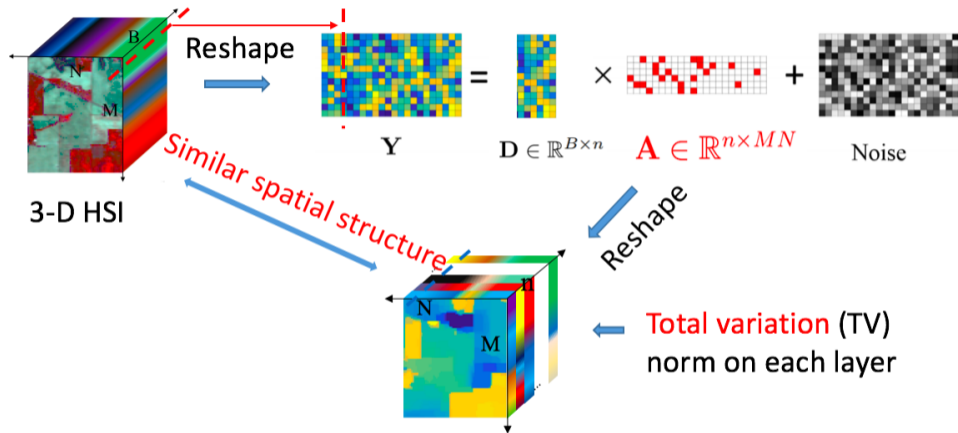
# Sketching



Reduces greatly the size of the problem!

P. A. Traganitis and G. B. Giannakis (2018). Sketched subspace clustering. IEEE Trans. Signal Process. [Traganitis and Giannakis, 2018]

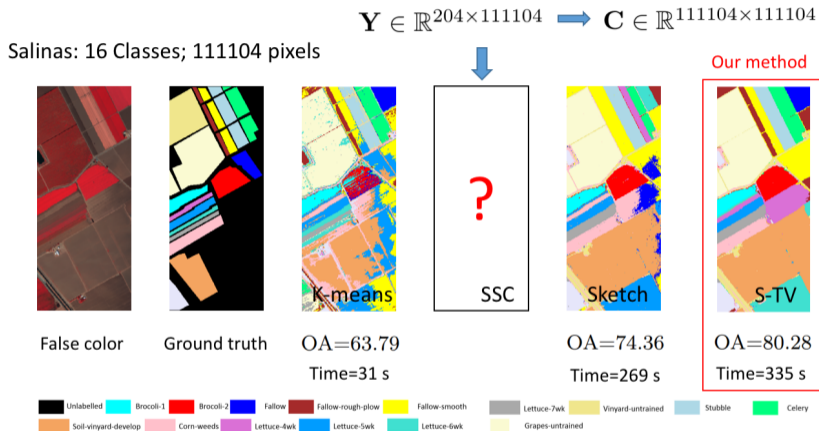
# Sketched Sparse Subspace Clustering for Hyperspectral Images



S. Huang, H. Zhang and A. Pižurica (2020).

Sketch-based Subspace Clustering of Hyperspectral Images. Remote Sensing.

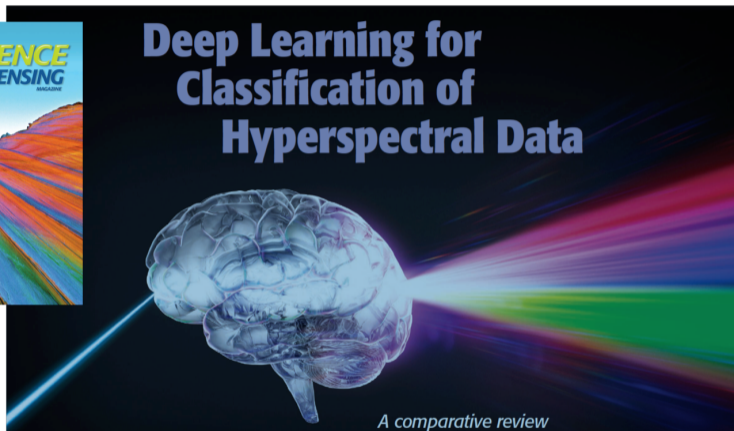
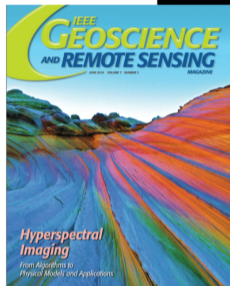
# Sketched Sparse Subspace Clustering for Hyperspectral Images



[Huang et al., 2020]



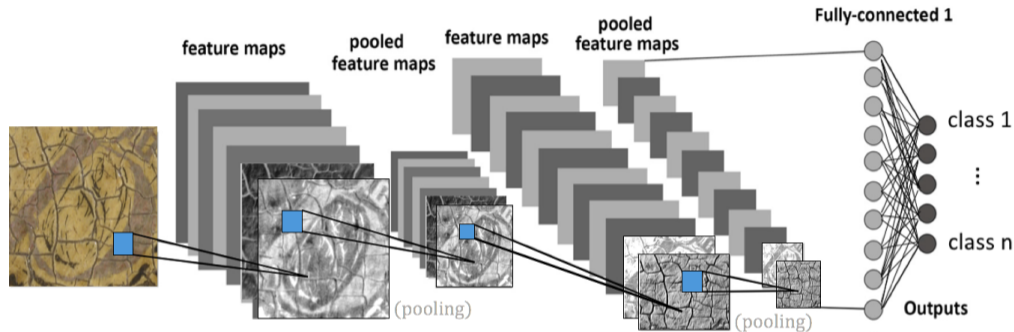
# Deep learning for HSI analysis



**NICOLAS AUDEBERT, BERTRAND LE SAUX, AND SÉBASTIEN LEFÈVRE**

N. Audebert, B. Le Saux, and S. Lefèvre, IEEE Geosc. Remote Sens. Mag., June 2019.

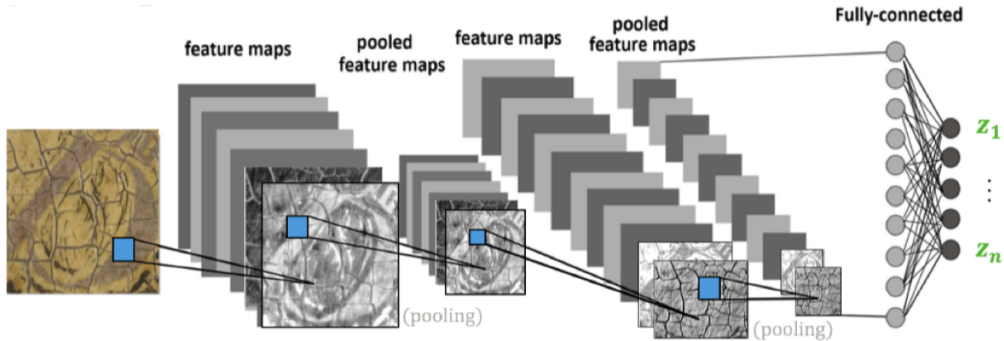
# Convolutional Neural Networks (CNN)



Output at location  $(i, j)$  of the  $k$ -th feature map in the  $l$ -th layer:

$$x_{i,j}^{l,k} = \sigma \left( \sum_{m=1}^M \sum_{p=0}^{H_l-1} \sum_{q=0}^{W_l-1} w_{p,q}^{l,k,m} x_{(i+p),(j+q)}^{(l-1),m} + b^{l,k} \right)$$

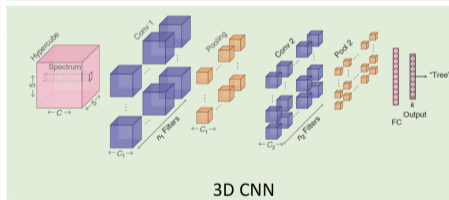
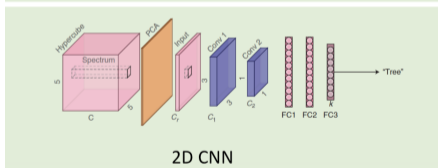
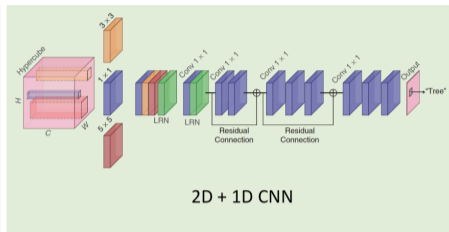
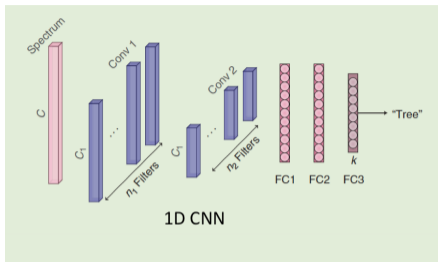
# Convolutional Neural Networks (CNN)



Predicted probabilities of class labels using the **softmax** rule:

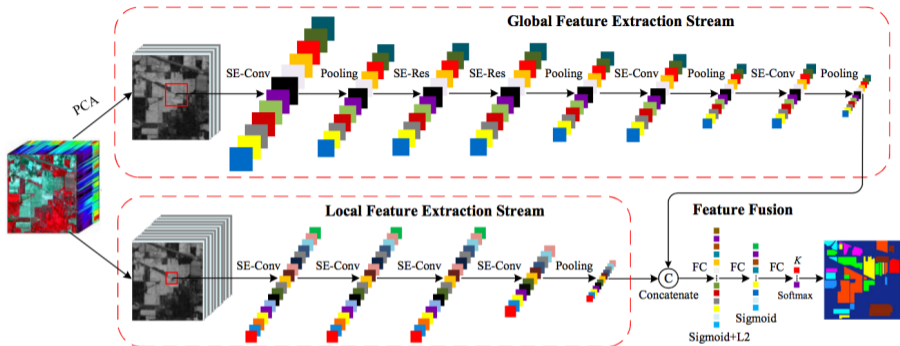
$$P(\text{class}(x_{i,j}) = c) = \frac{e^{z_c}}{\sum_k e^{z_k}}$$

# Deep learning models in HSI classification



N. Audebert, B. Le Saux, and S. Lefèvre. Deep Learning for Classification of Hyperspectral Data - A comparative Review. IEEE Geosc. Remote Sens. Mag., June 2019.

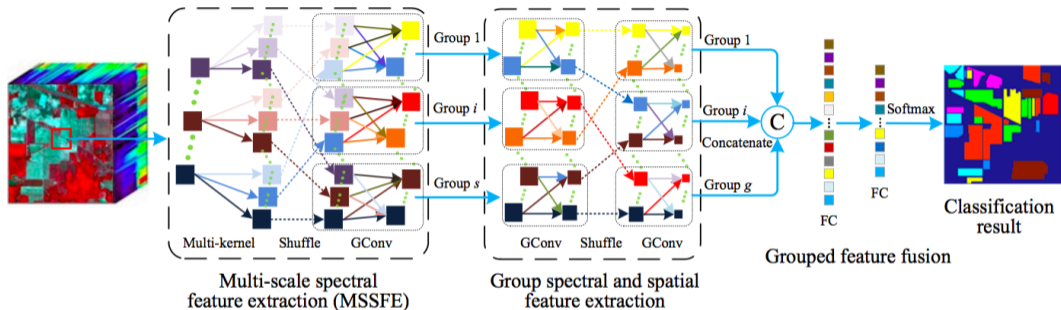
# Spectral-spatial feature fusion with two-stream CNN



Improving the performance in the case of limited labelled data.

X. Li, M. Ding and A. Pižurica. Deep Feature Fusion via Two-Stream Convolutional Neural Network for Hyperspectral Image Classification, IEEE Transactions on Geoscience and Remote Sensing, 2020. [Li et al., 2020]

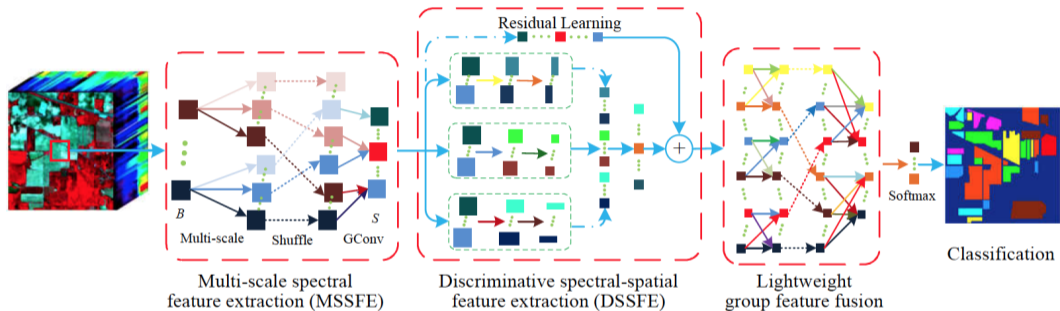
# Group CNN for HSI classification



Reducing the computational complexity - applicability to large scale data.

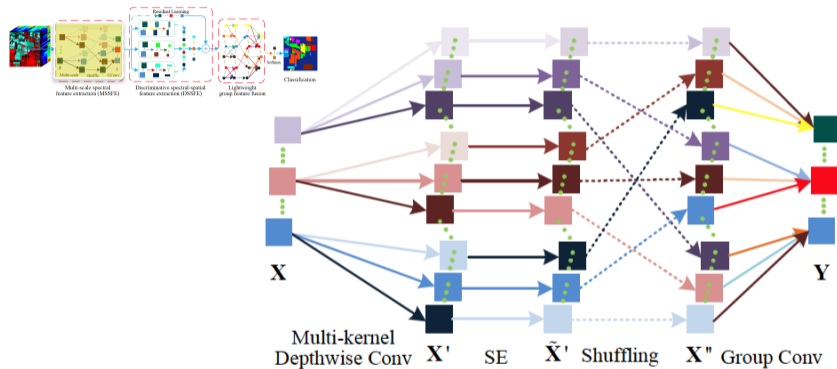
X. Li, M. Ding and A. Pižurica. Group Convolutional Neural Networks for Hyperspectral Image Classification, ICIP 2018.

# Full Group CNN (FGCNN)



X. Li, M. Ding and A. Pižurica. Full Group Convolutional Neural Networks for Robust Spectral-Spatial Feature Learning (2020). IEEE Trans. Image Process. (in review)

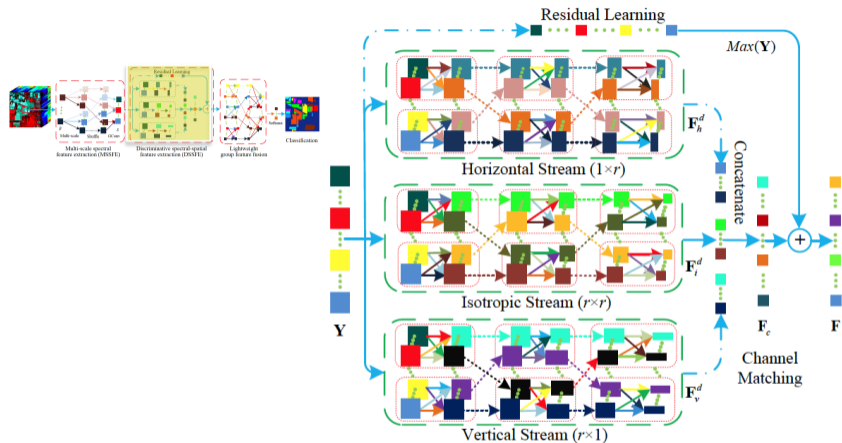
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X. Li, M. Ding and A. Pižurica. Full Group Convolutional Neural Networks for Robust Spectral-Spatial Feature Learning (2020). IEEE Trans. Image Process. (in review)

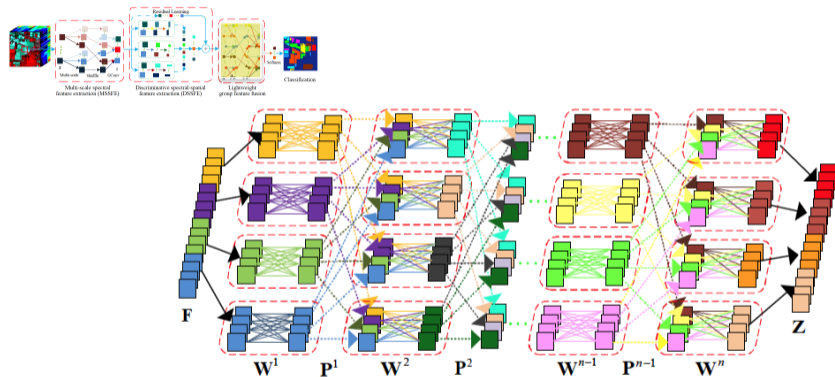


# Full Group CNN (FGCNN)



X. Li, M. Ding and A. Pižurica. Full Group Convolutional Neural Networks for Robust Spectral-Spatial Feature Learning (2020). IEEE Trans. Image Process. (in review)

# Full Group CNN (FGCNN)



X. Li, M. Ding and A. Pižurica. Full Group Convolutional Neural Networks for Robust Spectral-Spatial Feature Learning (2020). IEEE Trans. Image Process. (in review)

# The *Ghent Altarpiece*



Hubert and Jan Van Eyck, completed in 1432.

# The Ghent Altarpiece



Hubert and Jan Van Eyck, completed in 1432.

## The current restoration of the *Ghent Altarpiece*



# Ghent Altarpiece - Current Restoration Campaign

SCIENCE

The New York Times

## *A Master Work, the Ghent Altarpiece, Reawakens Stroke by Stroke*

By MILAN SCHREUER DEC. 19, 2016

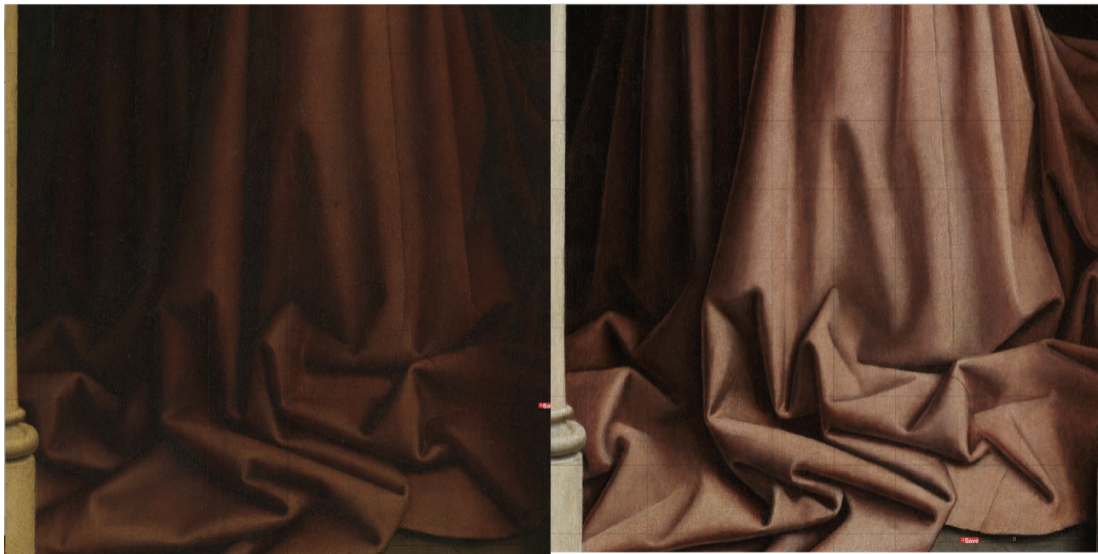


# Ghent Altarpiece restoration – Phase 1



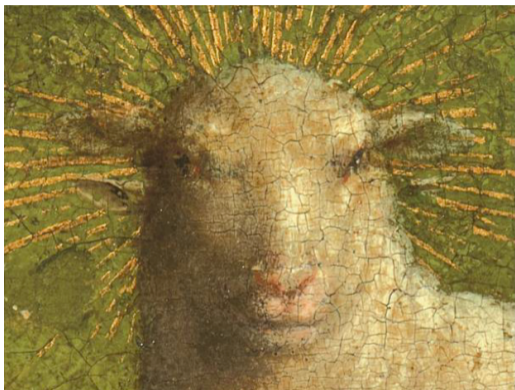
■ = Overpaint © KIK-IRPA

## Ghent Altarpiece restoration – Phase 1



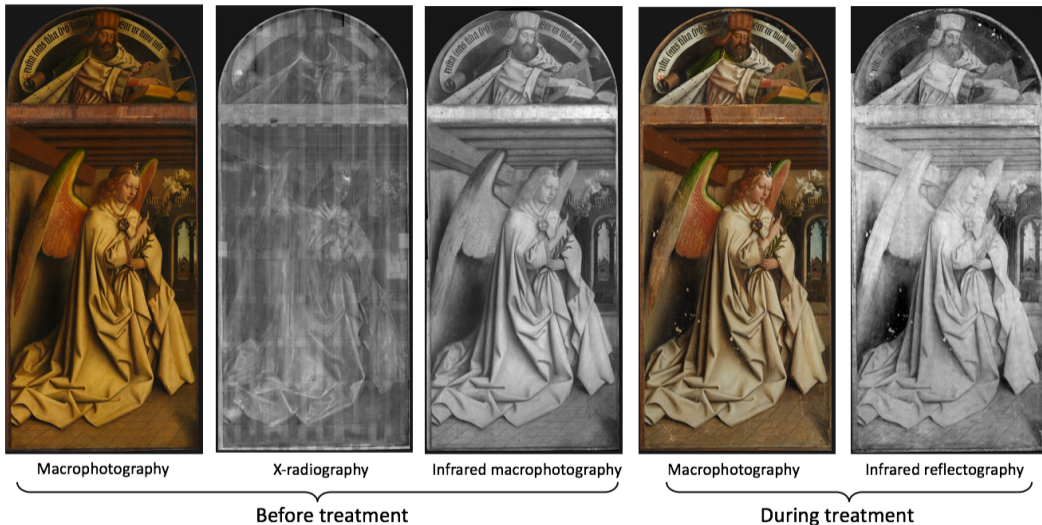


## Ghent Altarpiece restoration – Phase 2 (inner panels)



The *Mystic Lamb* – before and after the restoration.

# A multimodal approach



©Ghent, Kathedrale Kerkfabriek, Lukasweb

## A multiscale deep learning method for paint loss detection



Size:  $5954 \times 7546$ ; processed in  $< 1$  minute

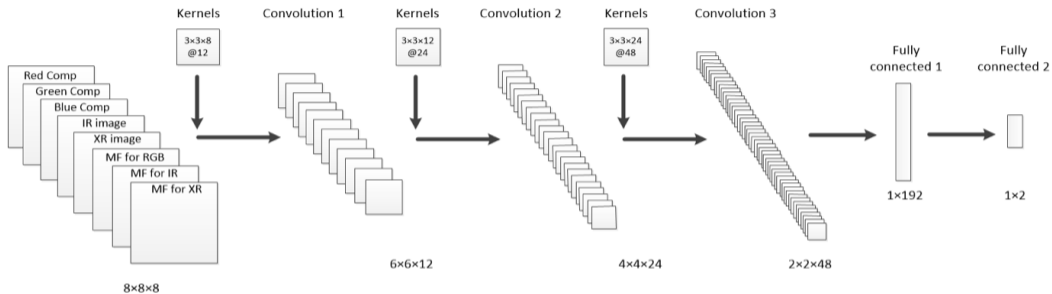
## Deep learning in crack detection



Crack detection in roads reported in [Lei et al,2016], [Cha et al, 2017].  
However, crack detection in paintings is much more challenging!

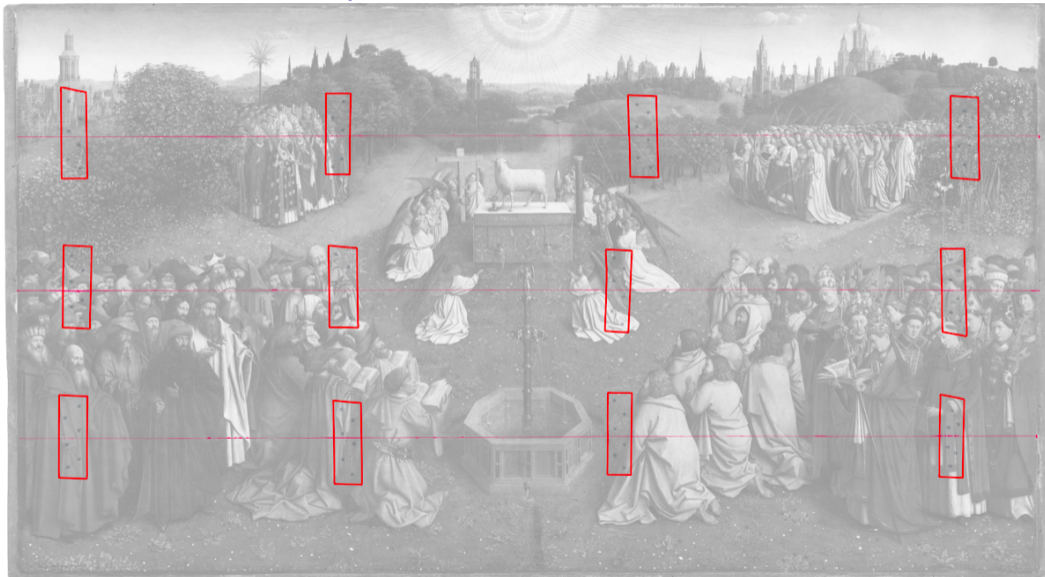


# A deep learning method for crack detection in paintings

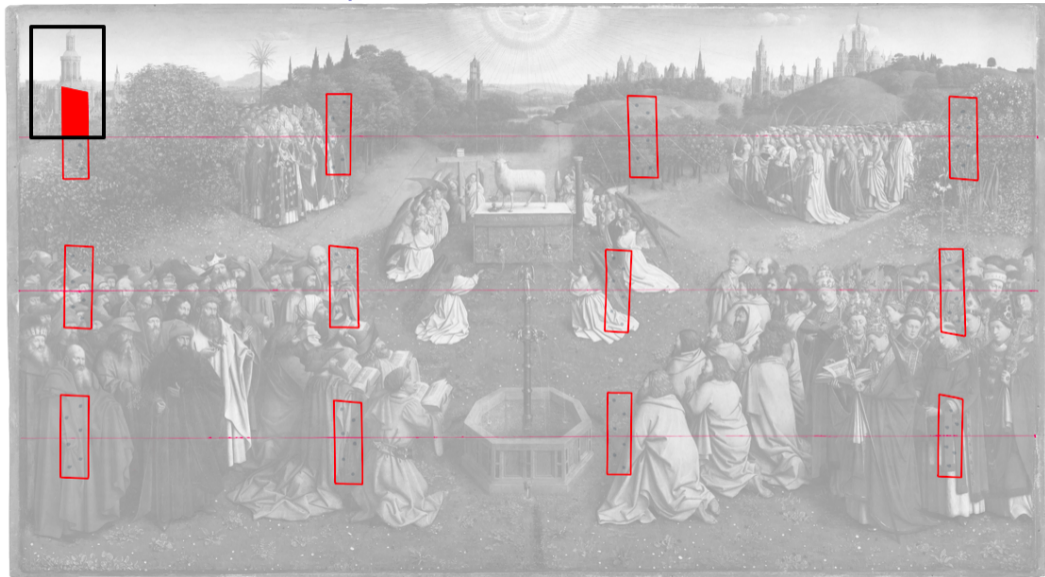


R. Sizyakin, B. Cornelis, L. Meeus, M. Martens, V. Voronin, and A. Pižurica (2018). A deep learning approach to crack detection in panel paintings. IP4AI.

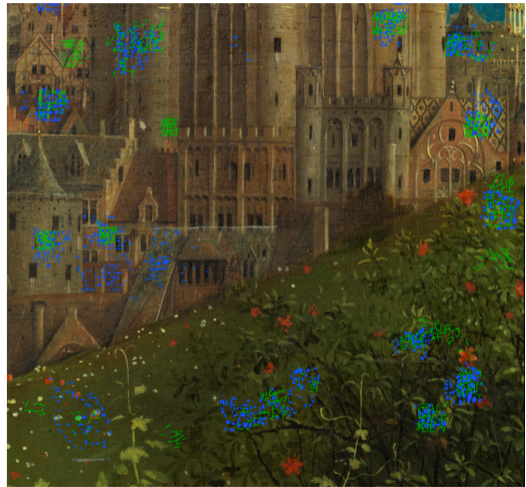
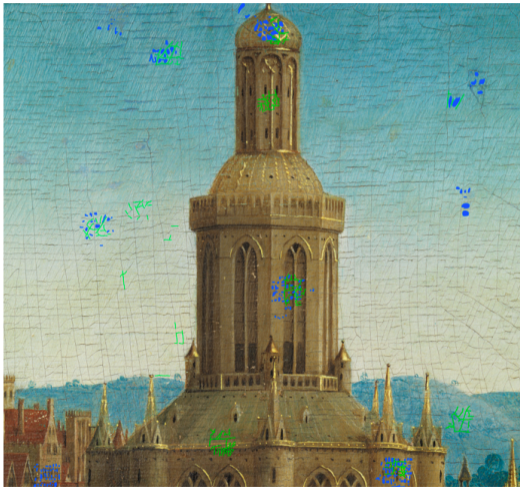
## Crack detection: Central panel



## Crack detection: Central panel

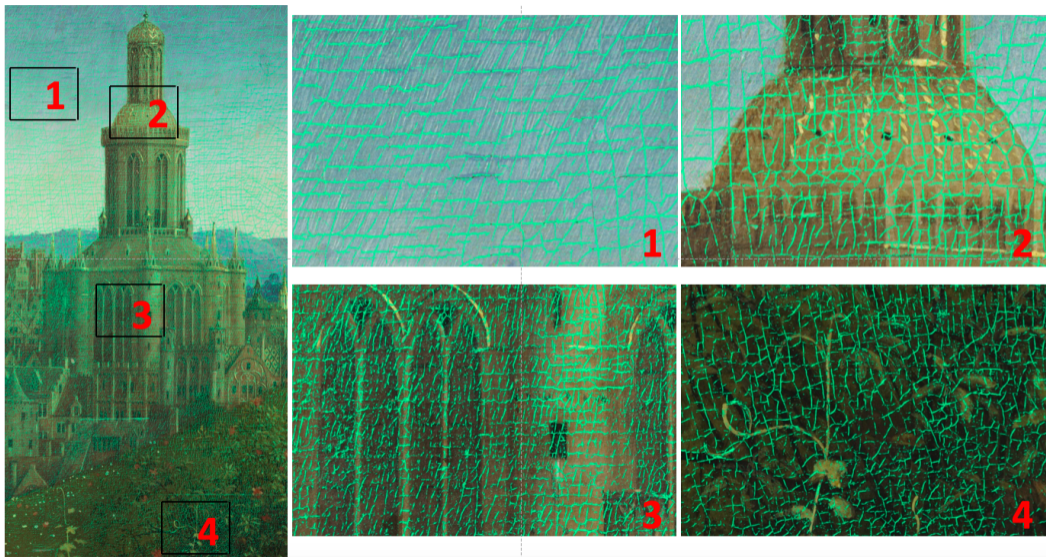


## Crack detection: Central panel

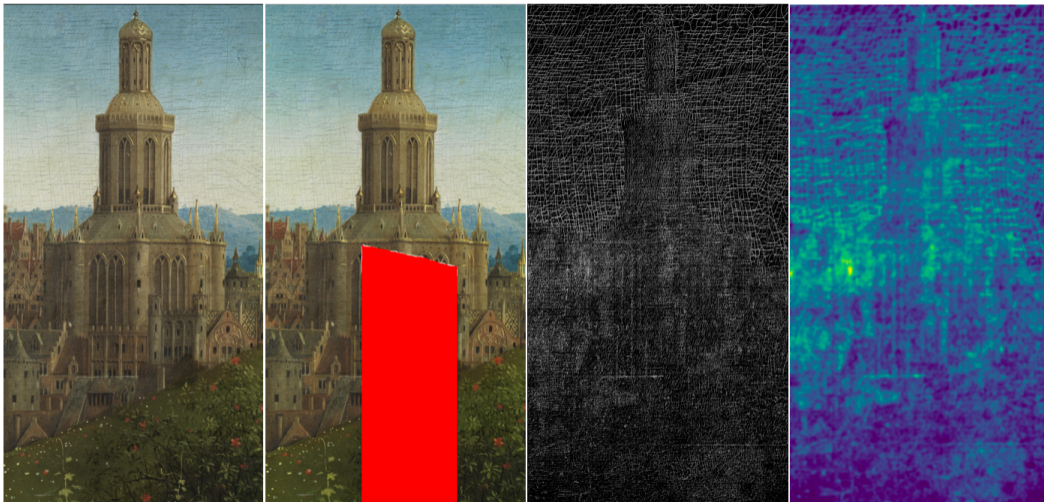




# Crack detection: Central panel

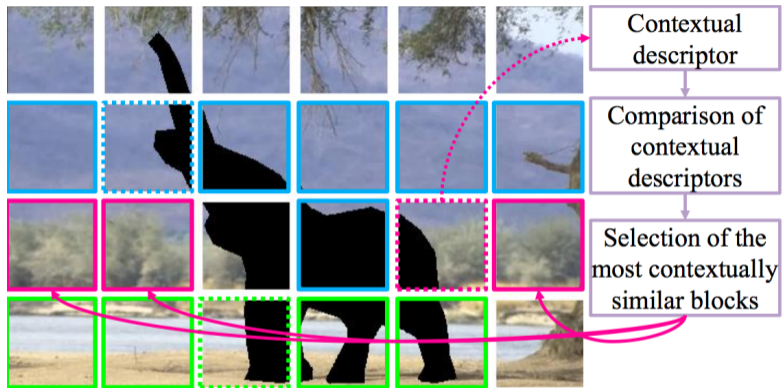


## Crack detection: Central panel



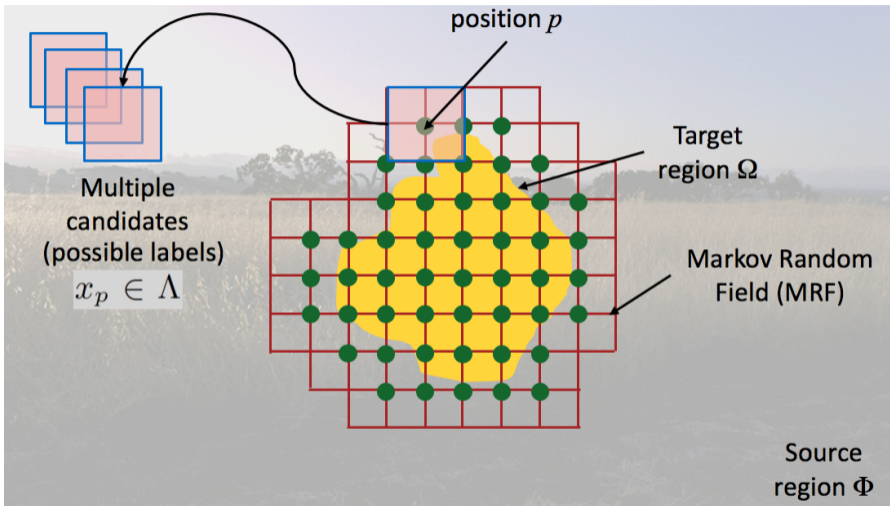
[Sizyakin et al., 2020] <https://ieeexplore.ieee.org/document/9072114>

# Context adaptive inpainting

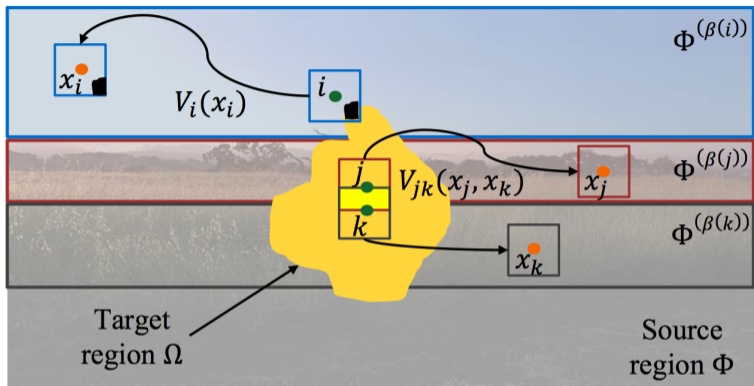


T. Ružić and A. Pižurica et al. Context-aware patch-based image inpainting using Markov random field modeling. *IEEE Transactions on Image Processing* 2015

# Global inpainting



# Global inpainting

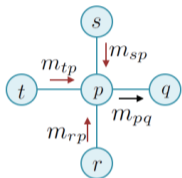


$$E(x) = \sum_{i \in \nu} V_i(x_i) + \sum_{\langle i, j \rangle \in \epsilon} V_{ij}(x_i, x_j), \quad (1)$$

[Komodakis and Tziritas, 2007], [Ružić and Pižurica, 2015]

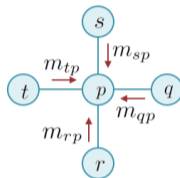
# Global inpainting

Messages



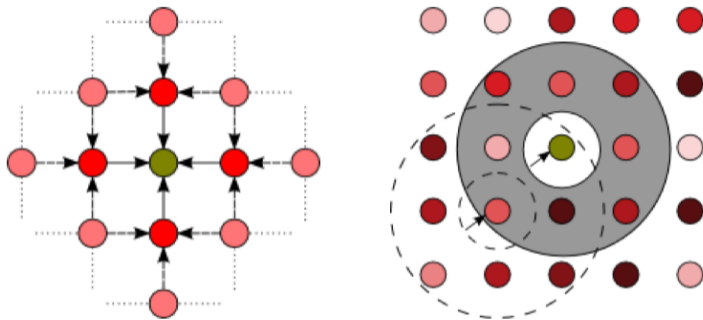
$$m_{pq}(x_q) = \min_{x_p \in \Lambda} \left\{ V_{pq}(x_p, x_q) + V_p(x_p) + \sum_{r: r \neq q, (r,p) \in \varepsilon} m_{rp}(x_p) \right\}$$

Beliefs



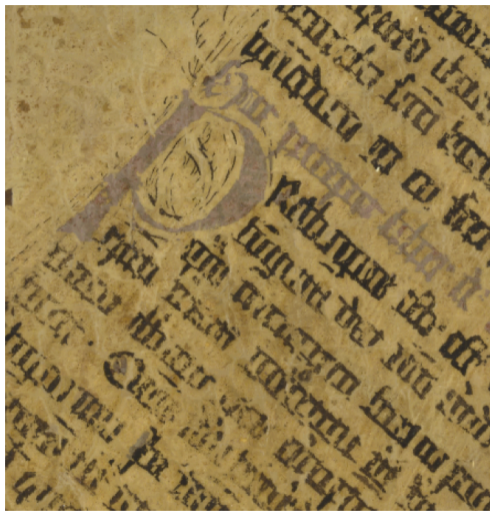
$$b_p(x_p) = -V_p(x_p) - \sum_{r: (r,p) \in \varepsilon} m_{rp}(x_p)$$

## Global inpainting: efficient inference



T. Ružić and A. Pižurica et al. Context-aware patch-based image inpainting using Markov random field modeling. *IEEE Transactions on Image Processing* 2015

## Crack inpainting



[Pižurica et al., 2015]



# Virtual Restoration



Left: original; Middle: automatic paint loss detection method [Meeus et al., 2019].  
Right: MRF-based inpainting method [Ružić and Pižurica, 2015]

# Research Group for Artificial Intelligence and Sparse Modelling - GAIM



Aleksandra Pizurica



Shaoguang Huang



Laurens Meeus



Nina Žižakić



Xian Li



Ting Zhao



Marko Panic



Meizhu Li



Srđan Lazendić



Roman Sizyakin



Hrvoje Leventić



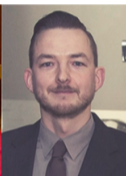
Nicolas Vercheval

GAIM (<https://gaim.ugent.be>) is part of the Department Telecommunications and Information Processing at the Faculty of Engineering of Ghent University.

# Collaborators



H  l  ne Dubois



Bart Devolder



Ljiljana Platiša



Tijana Ružić



Bruno Cornelis



Ann Doms



Max Martens



Ingrid Daubechies



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